

Follow the Sun and Go with the Wind: Carbon Footprint Optimized Timely E-Truck Transportation

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ABSTRACT

We study the carbon footprint optimization (CFO) of a heavy-duty e-truck traveling from an origin to a destination across a national highway network subject to a hard deadline, by optimizing path planning, speed planning, and intermediary charging planning. Such a CFO problem is essential for carbon-friendly e-truck operations. However, it is notoriously challenging to solve due to (i) the hard deadline constraint, (ii) positive battery state-of-charge constraints, (iii) non-convex carbon footprint objective, and (iv) enormous geographical and temporal charging options with diverse carbon intensity. Indeed, we show that the CFO problem is NP-hard. As a key contribution, we show that under practical settings it is equivalent to finding a generalized restricted shortest path on a stage-expanded graph, which extends the original transportation graph to model charging options. Compared to alternative approaches, our formulation incurs low model complexity and reveals a problem structure useful for algorithm design. We exploit the insights to develop an efficient dual-subgradient algorithm that always converges. As another major contribution, we prove that (i) each iteration only incurs polynomial-time complexity, albeit it requires solving an integer charging planning problem optimally, and (ii) the algorithm generates optimal results if a condition is met and solutions with bounded optimality loss otherwise. Extensive simulations based on real-world traces show that our scheme reduces up to 28% carbon footprint compared to baseline alternatives. The results also demonstrate that e-truck reduces 56% carbon footprint than internal combustion engine trucks.

CCS CONCEPTS

• Applied computing → Transportation; • Information systems → Spatial-temporal systems.

KEYWORDS

electric truck, carbon footprint, timely transportation,

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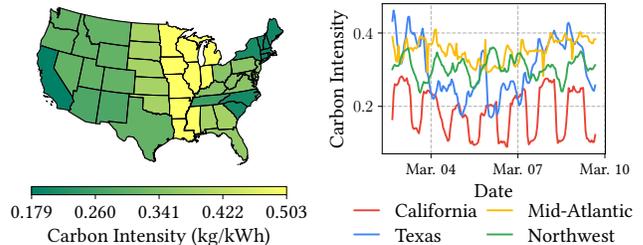


Figure 1: Spatial-temporal diversity of the carbon intensity (kg/kWh) in the US [2]. The whole country is divided to 13 regions. Each region includes one or multiple states. Carbon intensity is only provided for individual regions [2], thus one uniform color for all the states in a region.

	Coal	Natural gas	Petroleum	Renewable
Carbon Intensity (kg/kWh)	1.02	0.39	0.91	0
Total emission (tons)	7.86×10^8	6.35×10^8	1.6×10^7	0
Electricity (kWh)	7.73×10^{11}	1.62×10^{12}	1.75×10^{10}	7.92×10^{11}

Table 1: U.S electricity generation and resulting CO₂ emissions by major type of source in 2020 [20, Tab. 7.2a, Tab. 11.6]

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1 INTRODUCTION

In the United States, heavy-duty trucks deliver more than 10 billion tons of freight in 2021, representing 72.2% of total domestic tonnage shipped. 80.4% of the nation's freight bills are from trucking which amounts to 875 billion US dollars [5]. Despite their importance for the economy, heavy-duty trucks are a major source of Carbon Dioxide (CO₂) emission, which is tied to climate change. With only 4% of the total vehicle population, heavy-duty trucks produce 25% of the CO₂ emitted in the transportation sector, accounting for 8.8% of the total carbon emissions in the US [17]. To fight climate change, it is critical to de-carbonize the trucking industry.

Electrification of heavy-duty trucks is a promising endeavor with multi-facet benefits, including lower noise disturbance, better acceleration performance, better energy efficiency, and most notably, zero tailpipe emissions [11] with great potential to de-carbonize the trucking industry. However, while e-trucks do not generate direct CO₂ emission during the operation, charging e-trucks incurs positive *carbon footprint*, i.e., the CO₂ emission during the production of electricity to be consumed by the e-truck. It is thus essential to evaluate the carbon footprint of e-trucks in contrast to the tailpipe emission for ICE trucks [54].

	Speed Planning	Path Planning	Deadline Constraint	Charging Planning	Truck Type	Objective
RSP [30, 34, 38]	✗	✓	✓	N/A	ICE	Path cost
E2T2 [18, 36, 52, 54]	✓	✓	✓	N/A	ICE	Energy/Emission
many, e.g., [31]	✓	✗	✗	N/A	ICE	Energy
many, e.g., [46]	✓	✓	✗	✓	Electric/Hybrid	Time/Energy
many, e.g., [53]	✓	✗	✓	✗	Electric	Energy
This work	✓	✓	✓	✓	Electric	Carbon footprint

Table 2: Model comparison between this work and the existing work for truck operations.

In this paper, we study the carbon footprint optimization (CFO) of a heavy-duty e-truck traveling from an origin to a destination across a national highway network subject to a hard deadline, by exploring the complete design space of path planning, speed planning, and intermediary charging planning. Such a CFO problem is central to maximizing the environmental benefit brought by e-trucks. However, it is notoriously challenging to solve due to the following.

The hard deadline constraint. Transportation deadline is a common requirement in the trucking industry. In fact, timely delivery is not only necessary for perishable goods such as food [4], it is also commonly adapted in service-level agreements to guarantee delivery delay [3]. Moreover, transportation tasks on online platforms (e.g., Uber Freight [25]) are often associated with pickup/delivery time requirements, from which an end-to-end delivery deadline can be computed. Meanwhile, very often, considering deadline constraints can turn an easy problem, e.g., finding the fastest path between the origin and a destination, into an NP-hard counterpart [18].

Positive battery State of Charge (SoC) constraints. Range anxiety is a common issue for e-trucks due to their limited capacity. Careful planning to prevent battery depletion for an e-truck is thus necessary during the transportation task. However, this requirement adds strong couplings to the traveling decisions between successive road segments, thus largely complicating the problem.

Non-convex carbon footprint objective. We consider an e-truck incurs the carbon footprint objective during intermediary charging. End-use electricity often has a mix of different sources (e.g., coal, natural gas, petroleum, and renewable). Different sources have different carbon intensities (i.e., carbon footprint per unit electricity, unit: kg/kWh); see Tab. 1 for examples. Among those sources, renewable have notable zero carbon intensity and thus is an eco-friendly type of source. Meanwhile, renewable generation has a large variation in time and locations, resulting in spatial-temporal diversity of carbon intensity of electricity; see Fig. 1 for an illustration. The diverse carbon intensity, along with the nonlinear charging characteristics of the battery, makes the carbon footprint objective non-convex and challenging to deal with.

Enormous geographical and temporal charging options. Due to the fluctuating nature of the renewable, carbon intensity varies largely in both location and time. Jointly with path planning and speed planning, charging planning determines where and when to charge, how much to charge with diverse carbon intensity in different locations and time. The design space is combinatorial

in nature, with enormous options to consider, making the CFO problem uniquely challenging to solve.

Indeed, the CFO problem is more complicated and challenging than those in related studies for ICE truck and EV driving optimization and existing approaches are not directly applicable; see Sec. 2 for more discussions. In this paper, we carry out a comprehensive study of the problem and make the following **contributions**:

▷ We conduct the first study on *carbon footprint optimization* (CFO). We show that the problem is NP-hard. We then show that under practical settings, the CFO problem is equivalent to finding a generalized restricted shortest path on a stage-expanded graph, which extends the original transportation graph to incorporate charging options. Compared to alternative approaches, our novel formulation incurs low model complexity and reveals a problem structure useful for algorithm design.

▷ We then exploit the structured insights from the formulation to develop an efficient dual-subgradient algorithm that always converges. We show that in our approach, each iteration only incurs polynomial-time complexity in graph size, albeit it requires solving an integer charging planning problem optimally. We then further derive a condition under which our algorithm produces an optimal solution and a posterior performance bound when the condition is not satisfied.

▷ We carry out extensive numerical experiments using real-world traces over the US highway network to show the effectiveness of our approach in practice. The results show that our scheme reduces up to 28% carbon footprint as compared to a fastest-path alternative. We conduct a comparison between e-trucks and ICE trucks on their environmental impact. The results show that an e-truck achieves 56% carbon reduction compared to its ICE counterpart.

Due to the space limitation, all proofs are included in the technical report [48].

2 RELATED WORK

Energy-Efficient Timely Transportation (E2T2). E2T2 aims to find a path and its associated speed profile from an origin to a destination with minimum energy consumption, while satisfying a hard deadline [18, 36, 52]. It generalizes the NP-hard Restricted Shortest Path (RSP) [30, 34, 38] problem by introducing an additional design space of speed planning. E2T2 problem is first proposed in [18] and also shown to be NP-hard. E2T2 is then generalized to the scenario with multiple pickup/delivery locations with time windows in [36]. Another extension of E2T2 has been studied in [52], where the driver can strategically wait at the rest area for better traffic condition. However, all these studies above are for conventional internal

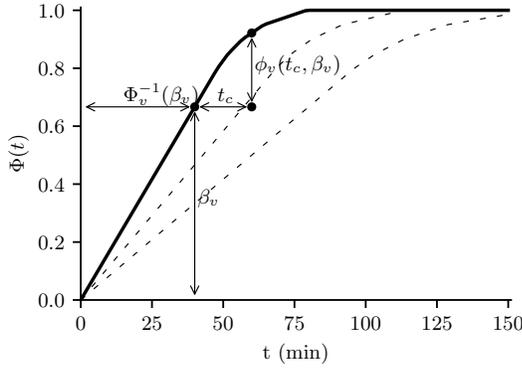


Figure 2: An example of charging function Φ , and the corresponding SoC difference function ϕ . The initial SoC is $\beta_v = 0.67$. After charging for 20 minutes, the increment of SoC $\phi(t_c, \beta_v) = 0.25$. The two dashed lines represent charging functions for different charging schemes.

combustion engine (ICE) trucks. In this work, we study the problem for electric trucks with a new objective of minimizing the carbon footprint, imposing unique challenges to the problem due to the coupling nature of the State of Charge (SoC) constraints. See Tab. 2 for a comparison of our work with related studies.

Path and Speed Planning for Electric Vehicle has long been an active research area. Path planning for EVs involves negative edge weights due to the regenerative system. Many variants of the RSP problem have been proposed for EVs by minimizing the energy consumption subject to a deadline [16, 37, 45], or by finding the fastest path subject to the battery capacity limit [6, 51]. However, all these works only focus on path planning and ignore the design space of speed planning. More recent works consider both path planning and speed planning [7, 8, 24, 29, 46]. For example, Baum et al. [8] seeks to find the fastest path with capacity limit by optimizing both path planning and speed planning for EVs without charging stops by the tradeoff function propagating technique. Strehler et al. [46] give theoretical insights to the path and speed planning problem for EVs and provide a fully polynomial time-approximation scheme (FPTAS) for the problem. Overall, all mentioned work and their approaches either do not apply to the CFO problem or incur large time complexity in the CFO problem; see also Table 3 and Sec. 3.3 for a comparison of conceivable approaches.

Variants of Vehicle Routing Problem (VRP). VRP generalizes the NP-hard traveling salesman problem (TSP), where the operator has a fleet of vehicles to fulfill the requirement of a set of customers. The variants of VRP for EV are considered in electric vehicle routing problem (EVRP) [19, 26, 41, 44]. Some other variants of VRP consider the environmental impacts of the routing decisions. For example, the green vehicle routing problem [21] considers VRP for alternative fuel vehicles. The pollution routing problem [10] considers minimizing the emission for conventional vehicles. The electric arc routing problem (eARP) [23] considers minimizing the total travel time on an energy-indexed graph. As a general observation, variants of VRP only consider path planning and are very complex. The existing methods for VRP do not scale to large-scale network.

3 PROBLEM FORMULATION

3.1 System Model

Transportation Graph and Energy Consumption. We model the highway system as a directed graph $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ where $\mathcal{V} = \mathcal{V}_r \cup \mathcal{V}_c$ is the set of nodes. Here \mathcal{V}_r denotes the nodes for real road segments and \mathcal{V}_c denotes the nodes for the charging stations. We denote $\mathcal{E} \subset \mathcal{V} \times \mathcal{V}$ the set of edges. For each road segment $e \in \mathcal{E}$, we denote its length by D_e and its minimum (resp. maximum) speed limit by R_e^{lb} (resp. R_e^{ub}). We define the minimum and maximum traveling time limit as $t_e^{lb} = D_e/R_e^{ub}$ and $t_e^{ub} = D_e/R_e^{lb}$.

Without loss of generality, we assume homogeneous road condition on a road segment $e \in \mathcal{E}$, e.g., the road grade. Given the weight of an e-truck and the road grade, we model its energy consumption rate over a road segment $e \in \mathcal{E}$ as a convex function of the traveling speed as justified in [18]: $f_e(r_e) : [R_e^{lb}, R_e^{ub}] \rightarrow \mathbb{R}$ (unit: kilowatts), where r_e is the traveling speed. Note that for e-trucks, f_e can take negative values over (downhill) road segments because of regenerative braking [6]. Because of the convexity of $f_e(\cdot)$, it suffices to assume that the e-truck travels on the road segment at constant speed [18, Lem. 1] with no optimality loss.¹ We further define an *energy consumption function* for an e-truck to traverse the road segment e as $c_e(t_e) = t_e \cdot f_e(D_e/t_e)$. We note that $c_e(\cdot)$ is a perspective function of $f_e(\cdot)$ with linear transformation. As such $c_e(t_e)$ must be convex in t_e [12].

E-Truck Charging. For each charging station node $v \in \mathcal{V}_c$, an e-truck can make two decisions: wait for $t_w \in [t_w^{lb}, t_w^{ub}]$ amount of time for lower carbon intensity and charge for $t_c \in [0, t_c^{ub}]$ amount of time. Here we use t_w^{lb} to denote the time overhead for an e-truck driver to stop and pay bills, etc. We denote the charging function at $v \in \mathcal{V}_c$ by a concave function $\Phi_v(t)$, which represents the charged SoC from zero after we charge for t amount of time.² Given an initial SoC β_v we can compute the increment of SoC after a charging time t_c as

$$\phi(t_c, \beta_v) = \Phi_v(\Phi_v^{-1}(\beta_v) + t_c) - \beta_v. \quad (1)$$

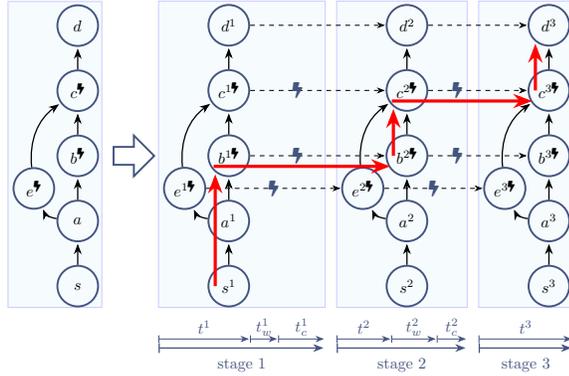
Here, Φ_v^{-1} is the inverse function of Φ_v ; see Fig. 2 for an illustration.

There could be multiple charging modes for e-trucks, e.g., fast charge and regular charge, which correspond to different charging functions (c.f. Fig. 2). Here, for simplicity, we assume the e-truck only applies the fast charging scheme at each charging station. We note that our approach can be easily extended to take multiple charging schemes into account. For example, we can model different charging schemes at a charging station by adding multiple charging nodes $i \in \mathcal{V}_c$ at the same location.

Carbon Intensity and Carbon Footprint. For each charging station $v \in \mathcal{V}_c$, we define a continuous carbon intensity function $\pi_v(\tau)$ (unit: kg/kWh) where τ is the arrival time instant at node v . We assume $\tau_0 = 0$ at the origin s for ease of the presentation. As illustrated in Fig. 1, the carbon intensity function $\pi_v(\cdot)$ largely

¹We ignore the acceleration/deceleration stage between road segments, as it usually occupies a small fraction of time/energy compared with that under the entire road segment.

²Most e-trucks use lithium-ion batteries, which are often charged with the constant-current constant voltage (CC-CV) scheme [43]. In the scheme, a battery is first charged by a constant current, and the SoC increases linearly until $\sim 80\%$ of the capacity. After that, a constant voltage is held to avoid overcharging degradation, causing the current to decrease and the SoC to increase concavely.



Property 1: The stages are connected by virtual charging edges.
Property 2: The time duration of each stage is variable.

Figure 3: An example of stage-expanded graph with $N = 2$ charging stops. Here, node b, c, e are charging stations in the original transportation graph.

varies in locations and time due to the geographical and temporal variation of the renewable generation. We note that the carbon-intensity information can be well forecasted at the hourly scale [39]. Given the carbon intensity function $\pi_v(\cdot)$, if the e-truck with initial SoC β_v starts charging at τ_v at station v and charges t_c time, the induced carbon footprint is

$$F_v(\beta_v, t_c, \tau_v) = \frac{1}{\eta} \int_0^{t_c} \pi_v(\tau_v + \xi) \frac{\partial \phi_v}{\partial t}(\xi, \beta_v) d\xi. \quad (2)$$

Here, $0 < \eta \leq 1$ is the charging efficiency of the battery. $\frac{\partial \phi_v}{\partial t}(\xi, \beta)$ is the left partial derivative with respect to t , which denotes the charging rate given the charging time ξ and initial SoC β . For charging at station $v \in \mathcal{V}_c$, the carbon footprint depends on the initial SoC β_v , the charging time t_c and the arrival time τ_v . It is the integral of the product of the price function and charging rate and thus nonlinear and non-convex.

3.2 Carbon Footprint Optimization Problem

We study the problem of minimizing the carbon footprint of an e-truck traveling from the origin $s \in \mathcal{V}$ to the destination $d \in \mathcal{V}$, subject to the hard deadline T and the SoC constraints. We consider that the e-truck with initial SoC β_0 and battery capacity B can take at most N charging stops during the trip. We assume N is a given parameter to our problem. In practice, it is reasonable to limit the number of charging stops in a trip for a good experience. The number is usually small, e.g., 3 or 4 for a 1500-mile e-truck transportation. In our simulation, we set the number of charging stops to be no more than eight.

A Stage-Expanded Graph. One of the challenges for formulating the CFO problem is the lack of the arrival time information and the arrival SoC information in the original transportation graph \mathcal{G} . Those information are essential for objective evaluation in the charging planning. To incorporate those information and mitigate this challenge, we consider a *stage-expanded graph*, which extends the original transportation graph to model the charging decisions.

In particular, we consider a stage-expanded graph $\mathcal{G}_s = (\mathcal{V}_s, \mathcal{E}_s)$ with $N + 1$ stages. Here \mathcal{V}_s contains $N + 1$ copies of original node, i.e., $\mathcal{V}_s = \{v^i : v \in \mathcal{V}, i \in \{1, \dots, N + 1\}\}$. The edge set \mathcal{E}_s keeps the original edges with additional connection between the same charging stations and destinations for two adjacent stages. That is,

$$\mathcal{E}_s = \{(u^i, v^i) : (u, v) \in \mathcal{E}, i \in \{1, \dots, N + 1\}\} \\ \cup \{(v^i, v^{i+1}) : v \in \mathcal{V}_c \cup \{d\}, i \in \{1, \dots, N\}\}.$$

When an e-truck at stage i decides to charge at a charging station $v \in \mathcal{V}_c$, we model it travels through a virtual stage transition edge (v^i, v^{i+1}) . At each stage, the e-truck travels towards the next charging station (or the destination), then wait and charge at the charging station and enter the next stage or stop at the destination. Note that the e-truck can charge less than N times, arrive the destination at stage $i < N + 1$ and then travel across stages through virtual edges between destinations and arrive the final stage. We provide an illustration in Fig. 3.

As we shall see in the following, the stage-expanded graph naturally incorporates the information of the arrival time and the arrival SoC, making it easier to model the charging decisions. We shall also discuss the benefits of such a stage-expanded graph and compare it conceivable alternatives later in Sec. 3.3 after we formulate the CFO problem.

Path and Charging Station Selection. A path in the stage-expanded graph consists of $N + 1$ subpaths connecting the source, no more than N charging stations and the destination. We use binary variables to represent the choice of charging stops at each stage and road segments in each subpath.

In particular, for each charging station $v \in \mathcal{V}_c$, we define a binary charging station selection variable $y_v^i \in \{0, 1\}$ and $y_v^i = 1$ means we want to choose charging station v as our i -th charging stop. For each subpath $i \in \{1, \dots, N + 1\}$ and road segment $e \in \mathcal{E}$, we define a binary path selection variable $x_e^i \in \{0, 1\}$ and $x_e^i = 1$ means we want to travel through road segment e for i -th subpath. For ease of presentation, we stack the variables $\vec{x}^i = \{x_e^i\}_{e \in \mathcal{E}}$, $\vec{x} = \{\vec{x}^i\}_{i=1}^{N+1}$ and $\vec{y}^i = \{y_v^i\}_{v \in \mathcal{V}_c}$, $\vec{y} = \{\vec{y}^i\}_{i=1}^{N+1}$. We define the feasible set of (\vec{x}, \vec{y}) as follows:

$$\mathcal{P} = \left\{ (\vec{x}, \vec{y}) \mid x_e^i \in \{0, 1\}, \forall e \in \mathcal{E}, i \in \{1, \dots, N + 1\} \right. \quad (3a)$$

$$\left. y_v^i \in \{0, 1\}, \forall v \in \mathcal{V}_c, i \in \{1, \dots, N + 1\} \right. \quad (3b)$$

$$\left. \sum_{e \in \text{Out}(v)} x_e^i - \sum_{e \in \text{In}(v)} x_e^i = y_v^{i-1} - y_v^i, \forall v \in \mathcal{V}, i \in \{1, \dots, N + 1\} \right. \quad (3c)$$

$$\left. \sum_{v \in \mathcal{V}} y_v^i = 1, \sum_{v \in \mathcal{V}_c} y_v^i = 1, \forall i \in \{1, \dots, N + 1\} \right. \quad (3d)$$

$$\left. y_s^0 = 1, y_d^{N+1} = 1 \right\}. \quad (3e)$$

Here, $\tilde{\mathcal{V}}_c = \mathcal{V}_c \cup \{s, d\}$. $\text{Out}(v)$ and $\text{In}(v)$ are the set of outgoing and incoming edges of node v , respectively. Constraint (3c) is the flow conservation requirement for each subpath. Constraint (3d) ensures that only one charging station is selected for each stage. Constraint (3e) defines that boundary case at the origin s and the

destination d . We remark that \mathcal{P} also covers path with charging stops less than N as we can choose the same charging stops at adjacent stages.

Speed and Charging Planning. We then define the decision variables for speed planning and charging planning. For each subpath i and road segment e , we denote the traveling time as t_e^i . We also denote by $t_w^{i,v}$, $t_c^{i,v}$ the waiting and charging time for charging station v as i -th charging stop. We also stack the variables as $\vec{t}^i = \{t_e^i\}_{e \in \mathcal{E}}$, $\vec{t}_w^i = \{t_w^{i,v}\}_{v \in \tilde{\mathcal{V}}_c}$, $\vec{t}_c^i = \{t_c^{i,v}\}_{v \in \tilde{\mathcal{V}}_c}$, $\vec{t} = \{\vec{t}^i, \vec{t}_w^i, \vec{t}_c^i\}_{i=0}^{N+1}$. The corresponding feasible set is given by

$$\mathcal{T} = \left\{ \vec{t} \mid t_e^i \in [t_e^{lb}, t_e^{ub}], \forall e \in \mathcal{E}, i \in \{1, \dots, N+1\}, \right. \quad (4a)$$

$$\left. t_w^{i,v} \in [t_w^{lb}, t_w^{ub}], t_c^{i,v} \in [0, t_c^{ub}], \forall v \in \tilde{\mathcal{V}}_c, i \in \{1, \dots, N\}, \right. \quad (4b)$$

$$\left. t_w^0 = t_c^0 = 0, \right\}. \quad (4c)$$

Time Constraints. We denote τ_v^i the moment of an e-truck entering the charging station v at i -th stop. It enables us to allocate the total allowed travel time T to the subpath at each stage. We also stack the variable as $\vec{\tau} = \{\tau_v^i\}_{v \in \tilde{\mathcal{V}}_c, i \in \{0, \dots, N+1\}}$ and its feasible set is given by

$$\mathcal{T}_\tau = \left\{ \vec{\tau} \mid \tau_v^i \in [0, T], \forall v \in \tilde{\mathcal{V}}_c, i \in \{0, \dots, N+1\} \right\}. \quad (5)$$

We consider the constraint that the traveling time and charging time are within the scheduled time window for i -th subpath, $i \in \{1, \dots, N+1\}$:

$$\begin{aligned} \delta_i^\tau(\vec{x}, \vec{y}, \vec{t}, \vec{\tau}) &= \sum_{e \in \mathcal{E}} x_e^i t_e^i + \sum_{v \in \tilde{\mathcal{V}}_c} y_v^{i-1} (t_w^{i-1,v} + t_c^{i-1,v}) \\ &\quad - \sum_{v \in \tilde{\mathcal{V}}_c} (y_v^i \tau_v^i - y_v^{i-1} \tau_v^{i-1}) \leq 0. \end{aligned} \quad (6)$$

Here, the first two terms are the traveling time on i -th subpath and the spent time for $(i-1)$ -th stop. The third term is the total scheduled time duration between $(i-1)$ -th stop and i -th stop.

SoC Constraints. It is complicated to keep track of the SoC at each road segment. In practice, we see that the regenerative braking only contributes a small fraction of energy to the e-truck [47]. With such a practical observation, we show that with a small reservation requirement at the SoC when entering a charging stop at a stage, it is sufficient to guarantee the positive SoC in the entire subpath at that stage.

In particular, we denote by β_v^i the SoC entering charging station v at i -th stop. We stack the variable as $\vec{\beta} = \{\beta_v^i\}_{v \in \tilde{\mathcal{V}}_c, i \in \{0, \dots, N+1\}}$, and its feasible set is given by

$$\mathcal{S}_\alpha = \left\{ \vec{\beta} \mid \beta_v^i \in [\alpha B, B], \forall v \in \tilde{\mathcal{V}}_c, i \in \{0, \dots, N+1\}, \beta_s^0 = \beta_0 \right\}. \quad (7)$$

Here, $\alpha \in [0, 1)$ denotes the ratio of a conservative lower bound for SoC when an e-truck entering a charging station. We consider the initial SoC at the source as β_0 .

We define the SoC constraint that the e-truck does not run out of battery when entering i -th stop:

$$\begin{aligned} \delta_i^\beta(\vec{x}, \vec{y}, \vec{t}, \vec{\beta}) &= \sum_{e \in \mathcal{E}} x_e^i c_e(t_e^i) + \sum_{v \in \tilde{\mathcal{V}}_c} y_v^i \beta_v^i \\ &\quad - \sum_{v \in \tilde{\mathcal{V}}_c} y_v^{i-1} (\beta_v^{i-1} + \phi_v(\beta_v^{i-1}, t_c^{i-1,v})) \leq 0. \end{aligned} \quad (8)$$

Here, the first term is the total energy consumption for i -th subpath, the second term is the SoC when the e-truck enters the i -th stop, the third term is the SoC when the e-truck leaves the $(i-1)$ -th stop.

We show that a small α is sufficient to ensure SoC feasibility during a subpath, as long as the harvested energy due to regenerative brake is relatively small.

LEMMA 3.1. *Let an e-truck travels along a subpath with n road segments to a charging stop, along with its energy consumption on each road segment $[c_1, \dots, c_n]$. If the harvested energy is relatively small and satisfies*

$$\frac{1}{2} \sum_{i=1}^n (|c_i| - c_i) \leq \frac{\alpha}{2(1-\alpha)} \sum_{i=1}^n c_i, \quad (9)$$

then the SoC at the charging stop being no less than $\alpha \cdot B$ implies that the e-truck always has a non-negative SoC during this subpath.

Note that the harvested energy (i.e., left hand side of (9)) for an e-truck traveling across national highway system is indeed small [47]. Because the maximum permissible grade along the US highway is no larger than 6% [28], there is little energy that can be harvested. Meanwhile, our simulation in Sec. 5 shows that $\alpha = 0.05$ is sufficient to ensure non-negative SoC for most of the instances in our simulation. Moreover, it also shows that it incurs a small performance gap by comparing it with a lower bound where α is set as zero.

Problem Formulation. To this end, we are ready to formulate the *Carbon Footprint Optimization* (CFO) problem as follows:

$$\text{CFO : } \min \sum_{i=1}^N \sum_{v \in \tilde{\mathcal{V}}_c} y_v^i F_v(t_c^{i,v}, t_w^{i,v}, \beta_v^i, \tau_v^i) \quad (10a)$$

$$\text{s.t. } \delta_i^\tau(\vec{x}, \vec{y}, \vec{t}, \vec{\tau}) \leq 0, \forall i \in \{1, \dots, N+1\} \quad (10b)$$

$$\delta_i^\beta(\vec{x}, \vec{y}, \vec{t}, \vec{\beta}) \leq 0, \forall i \in \{1, \dots, N+1\} \quad (10c)$$

$$\text{var. } (\vec{x}, \vec{y}) \in \mathcal{P}, \vec{\beta} \in \mathcal{S}_\alpha, \vec{\tau} \in \mathcal{T}_\tau, \vec{t} \in \mathcal{T}. \quad (10d)$$

Here, we aim to minimize the carbon footprint objective (10a). Constraint (10b) is the time scheduling constraint for each subpath. Constraints (10c) is the SoC constraints for each subpath.

We give the hardness result of the problem in the follow theorem.

THEOREM 3.2. *CFO is NP-hard.*

The NP-hardness of the CFO problem comes from the fact that a special case of the CFO problem is PASO problem [18] that considers the path planning and speed planning for energy-efficient timely transportation with ICE trucks.

Graph Model in Formulation	Problem	Model Complexity	Algorithm	Complexity	Optimality
Original graph	MIP	$O(\mathcal{V} + \mathcal{E})$	Branch and bound	Exponential to $ \mathcal{V} $ and $ \mathcal{E} $	Optimal
Battery-expanded graph	MILP [†]	$O(B/\epsilon(\mathcal{V} + \mathcal{E}))$	Branch and cut	Exponential to $ \mathcal{V} $, $ \mathcal{E} $, and B/ϵ	$O(\epsilon)$ to optimal
Time-expanded and battery-expanded graph	Shortest Path	$((T \cdot B)/\epsilon^2)(\mathcal{V} + \mathcal{E})$	Bellman-Ford	Polynomial to $ \mathcal{V} $, $ \mathcal{E} $, T/ϵ and B/ϵ	$O(\epsilon)$ to optimal
Our stage-expanded graph	Generalized RSP [‡]	$O(N(\mathcal{E} + \mathcal{V}))$	Dual subgradient	Polynomial to $ \mathcal{V} $, $ \mathcal{E} $, and N	Posterior bound

[†]: Provided that the carbon intensity function is approximated by a piecewise linear function. [‡]: RSP stands for restricted shortest path.

Message 1: Compared with battery-expanded graphs, our stage-expanded graph has a low model complexity because the number of stages $N \leq 10$ in practice.

Message 2: Compared with MIP formulations, our formulation reveals an elegant problem structure that leads to an efficient algorithm with favorable performance.

Table 3: Comparison of conceivable problem modelings, formulations, and algorithms for the CFO problem.

3.3 Remark on Challenges and Novelty

We first remark on four outstanding challenges of the CFO problem, after which we discuss the novelty of our formulation and its significance for tackling those challenges.

Remark on Challenges. The first challenge comes from optimal path planning and speed planning under the hard deadline constraint, which already makes the problem NP-hard. This challenge exists in both the CFO problem and the E2T2 problem for ICE trucks, e.g., [18]. The following three challenges are unique to e-truck and CFO.

The second challenge is the positive battery SoC requirement for each road segment, which adds strong couplings to the problem. One of the conventional ways is to explicitly define variables and constraints on each road segment (c.f., EVRP [41]) and obtain a large Mixed-Integer Programming (MIP). However, the resulting MIP is still challenging to solve because general-purpose methods usually do not scale well on MIP. We mitigate this challenge in our formulation with a key observation (Lemma 3.1) that it is sufficient to restrict the SoC only when entering each charging stop (and the destination) by a conservative lower bound, i.e., (8). As reported in Sec. 5, such simplification only incurs a small performance loss.

The third challenge comes from the non-convex objective, which is unique to the CFO problem. The objective is time-varying and highly non-convex with respect to τ due to the fluctuating nature of renewable. Large-scale non-convex problems are in general challenging to solve. Our problem formulation reveals an elegant problem structure that allows us to decompose the large non-convex problem into a number of significantly less-complex subproblems, which can be efficiently solved by global optimization tools, as we will show in Sec. 4.

The last challenge comes from enormous geographical and temporal charging options with diverse carbon intensity. The charging station selection configuration space has a combinatorial nature. A straightforward search over locations results in an exponential runtime with respect to N . To tackle this challenge, our formulation extends the transportation graph to a stage-expanded graph to model charging options. This extension significantly reduces the

searching space to a polynomial number and allows us to systematically search charging stations with constraint-respect costs via Lagrangian relaxation.

Remark on Novelty. Overall, those four challenges make the CFO problem notoriously challenging to solve. In the following, we remark the novelty of our approach by comparing our approach with several conceivable alternatives that are applicable to the CFO problem. We summarize the comparison in Tab. 3.

The first direction of alternatives (c.f., the first row and the second row in Tab. 3) resorts to directly formulate the CFO problem as a Mixed Integer Program (MIP) and solve it with general-purpose methods (e.g., branch and bound). However, the resulting MIP is still challenging to solve. The general-purpose methods usually do not scale well to large problems as they do not carefully explore the problem structure.

The second direction of alternative expands the graph with discretized state β and τ (c.f. the third row in Tab. 3). Once the expanded graph is constructed, the CFO problem can be transformed to a shortest path problem on the expanded graph. However, the graph is $(T \cdot B)/\epsilon^2$ times of the original graph, making the approach fail to scale to large networks with favorable accuracy.

In contrast, our formulation in (10) enjoys the benefits for the both worlds. It has a low-complexity stage-expanded graph model, which does not involve discretizing the time or SoC. Moreover, the formulation reveals an elegant problem structure for effective algorithm design. In the next section, we shall exploit the understanding and design an efficient dual-subgradient method that has good theoretical and empirical performance.

4 AN EFFICIENT ALGORITHM WITH PERFORMANCE GUARANTEE

In this section, we develop an efficient dual-subgradient algorithm for solving the CFO problem with performance guarantee, by exploring the structural insights of the formulation in (10).

4.1 The Dual Problem

We obtain a partially-relaxed dual problem of CFO in (10) by relaxing the constraints (10b) and (10c) with dual variable λ_i^τ and λ_i^β ,

respectively. The Lagrangian function is given by

$$L(\vec{x}, \vec{y}, \vec{t}, \vec{\beta}, \vec{\tau}, \vec{\lambda}) = \sum_{i=1}^N \sum_{v \in \mathcal{V}_c} F_v(t_c^{i,v}, t_w^{i,v}, \beta_v^i, \tau_v^i) + \sum_{i=1}^{N+1} \lambda_i^\tau \delta_i^\tau(\vec{x}, \vec{y}, \vec{t}, \vec{\tau}) + \sum_{i=1}^{N+1} \lambda_i^\beta \delta_i^\beta(\vec{x}, \vec{y}, \vec{t}, \vec{\beta}),$$

where $\vec{\lambda} = (\vec{\lambda}^\beta, \vec{\lambda}^\tau)$. The corresponding dual problem is given by

$$\max_{\vec{\lambda} \geq 0} D(\vec{\lambda}) = \max_{\vec{\lambda} \geq 0} \min_{\substack{(\vec{x}, \vec{y}) \in \mathcal{P}, \\ \vec{\beta} \in \mathcal{S}_\alpha, \vec{\tau} \in \mathcal{T}_\tau, \vec{t} \in \mathcal{T}}} L(\vec{x}, \vec{y}, \vec{t}, \vec{\beta}, \vec{\tau}, \vec{\lambda}). \quad (11)$$

Given $\vec{\lambda}$, we observe the problem of $D(\vec{\lambda})$ is a two-level problem where the inner level consists of a number of small subproblems and the outer level is a combinatorial problem over the feasible set \mathcal{P} . That is,

$$D(\vec{\lambda}) = D_1(\vec{\lambda}) + \min_{(\vec{x}, \vec{y}) \in \mathcal{P}} \left(\sum_{i=1}^{N+1} \sum_{e \in \mathcal{E}} x_e^i \underbrace{\min_{t_e^i \in [t_e^l, t_e^u]} g_e^i(\vec{\lambda}, t_e^i)}_{\text{speed planning}} \right) + \sum_{i=1}^N \sum_{v \in \mathcal{V}_c} y_v^i \underbrace{\min_{\substack{t_c^{i,v} \in [0, t_c^{ub}], t_w^{i,v} \in [t_w^l, t_w^{ub}], \\ \beta_v^i \in [\beta^l, B], \tau_v^i \in [0, T]}} h_v^i(\vec{\lambda}, t_c^{i,v}, t_w^{i,v}, \beta_v^i, \tau_v^i)}_{\text{charging planning}}, \quad (12a)$$

$$\quad (12b)$$

where $D_1(\vec{\lambda}) = -\lambda_{N+1}^\tau T - \beta_0 \lambda_1^\beta$ is a constant for any given $\vec{\lambda}$ and

$$g_e^i(\vec{\lambda}, t_e^i) = \lambda_i^\tau t_e^i + \lambda_i^\beta c^e(t_e^i) \quad (13)$$

represents the trade-off between the traveling time t_e^i and the energy consumption $c_e(t_e^i)$ for each road segment $e \in \mathcal{E}$. The function

$$h_v^i(\vec{\lambda}, t_c^{i,v}, t_w^{i,v}, \beta_v^i, \tau_v^i) = F_v(t_c^{i,v}, t_w^{i,v}, \beta_v^i, \tau_v^i) + \lambda_{i+1}^\tau (t_w^{i,v} + t_c^{i,v}) \quad (14a)$$

$$+ (\lambda_{i+1}^\tau - \lambda_i^\tau) \tau_v^i + (\lambda_i^\beta - \lambda_{i+1}^\beta) \beta_v^i - \lambda_{i+1}^\beta \phi_v(\beta_v^i, t_c^{i,v}) \quad (14b)$$

represents the trade-off between the objective and the constraints. Next, we define

$$w_e^i(\vec{\lambda}) = \min_{t_e^i \in [t_e^l, t_e^u]} g_e^i(\vec{\lambda}, t_e^i), \quad (15a)$$

$$\sigma_v^i(\vec{\lambda}) = \min_{\substack{t_c^{i,v} \in [0, t_c^{ub}], t_w^{i,v} \in [t_w^l, t_w^{ub}], \\ \beta_v^i \in [\alpha B, B], \tau_v^i \in [0, T]}} h_v^i(\vec{\lambda}, t_c^{i,v}, t_w^{i,v}, \beta_v^i, \tau_v^i). \quad (15b)$$

Here, $w_e^i(\vec{\lambda})$ can be computed by solving a single-variable convex optimization problem because $g_e^i(\vec{\lambda}, t_e^i)$ is convex with respect to t_e^i . The computation of $\sigma_v^i(\vec{\lambda})$ requires more effort, where we need to solve a 4-variable non-convex optimization problem over box constraints. Fortunately, the dimension of the subproblem (15b) is fixed. Therefore, we can obtain $\sigma(\vec{\lambda})$ in $O(M^4/\epsilon_1^4)$ with a Branch and Bound (BnB) scheme [13]. Here $M = \max\{t_c^{ub}, t_w^{ub}, B, T\}$ is the diameter of the box constraint in subproblem (15b) and ϵ_1 is the accuracy.

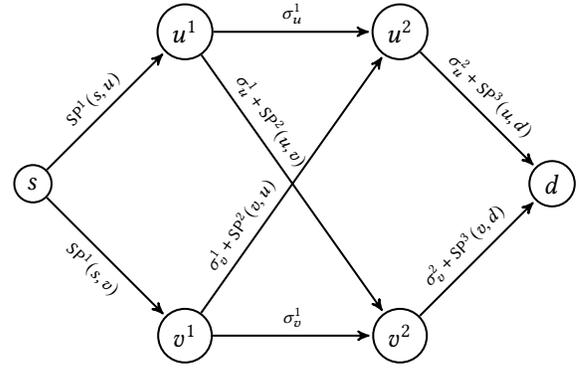


Figure 4: An example of the extended graph with $N = 2$. In the original graph, we have two charging stations u and v .

Solving the Outer Level Problem. After solving the inner level subproblems (15a) and (15b), the dual function can be written as follows:

$$D(\vec{\lambda}) = D_1(\vec{\lambda}) + \min_{(\vec{x}, \vec{y}) \in \mathcal{P}} \sum_{i=1}^{N+1} \sum_{e \in \mathcal{E}} w_e^i(\vec{\lambda}) x_e^i + \sum_{i=1}^N \sum_{v \in \mathcal{V}_c} \sigma_v^i(\vec{\lambda}) y_v^i. \quad (16)$$

The problem in (16), at first glance, is an integer linear program (ILP) which is in general challenging to solve. However, after exploring the problem structure, we can see that each charging station v is associated with a cost σ_v^i if it is the i -th charging stop, and each road segment e is with a cost w_e^i if it is in i -th subpath. Our goal is to find N charging stops and $N + 1$ subpaths with the minimum total cost. We observe that given any charging station selection, optimal subpaths can be determined by the shortest paths. Correspondingly, we can construct an extended graph consisting of N layers of charging stations with cost σ_v^i and edges between any two nodes in the consecutive layers with weight determined by the shortest paths. We can then find the optimal charge stop selection by the shortest path on the extended charging station graph. This idea leads to a novel two-level shortest path algorithm.

In particular, we construct an extended graph $\mathcal{G}_{ex} = (\mathcal{V}_{ex}, \mathcal{E}_{ex})$, where the node set \mathcal{V}_{ex} contains s, d and N copies of charging stations, i.e.,

$$\mathcal{V}_{ex} = \{s, d\} \cup \{v^i \mid v \in \mathcal{V}_c, i \in \{1, \dots, N\}\}. \quad (17)$$

For each $u, v \in \mathcal{V}_c$ and $i \in \{1, \dots, N\}$, we construct an edge between u^i and v^{i+1} with cost $\sigma_u^i(\vec{\lambda}) + SP^{i+1}(u, v)$ where $SP^{i+1}(u, v)$ is the cost of shortest path between (u, v) on the original graph \mathcal{G} with weight $w_e^{i+1}(\vec{\lambda})$. Similarly, we construct edges $(s, v^1), \forall v \in \mathcal{V}_c$ with weights $SP^1(s, v)$ and construct edges $(u^N, d), \forall u \in \mathcal{V}_c$ with weights $\sigma_u^N + SP^{N+1}(u^N, d)$. By construction, we have the following lemma:

LEMMA 4.1. *A shortest path on \mathcal{G}_{ex} corresponds to an optimal solution to ILP problem in (16).*

Hence, we can solve the ILP problem (16) by applying a shortest path algorithm to the extended graph \mathcal{G}_{ex} with low time complexity. Overall, given any $\vec{\lambda}$, we can compute the value of $D(\vec{\lambda})$ by first solving a number of subproblems (15a) and (15b) and then solving the outer problem (16) with shortest algorithms on an extended graph.

Algorithm 1 A Dual Subgradient Method

```

1: Initialization:  $\text{sol} \leftarrow \text{NULL}$ ,  $\vec{\lambda}[1] \leftarrow 0$ 
2: for  $k \leftarrow 1$  to  $K$  do
3:   Compute  $\text{sol}^+$  with  $\vec{\lambda}[k]$  by solving problem (12)
4:   if  $\delta_i^\beta[k] = 0$  and  $\delta_i^\tau[k] = 0, \forall i \in \{1, \dots, N+1\}$  then
5:     return  $\text{sol} \leftarrow \text{sol}^+$ 
6:   if  $\delta_i^\beta[k] \leq 0$  and  $\delta_i^\tau[k] \leq 0, \forall i \in \{1, \dots, N+1\}$  and  $\text{sol}^+$ 
   has less objective then
7:      $\text{sol} \leftarrow \text{sol}^+$ 
8:   Compute  $\vec{\lambda}[k+1]$  according to (18).
9: return  $\text{sol}$ 

```

4.2 A Dual Subgradient Algorithm

We use the dual subgradient method to iteratively update the dual variable $\vec{\lambda}$. In particular, we denote by $\vec{\lambda}[k]$ the dual variable at k -th iteration. Then we update the dual variable as follows:

$$\lambda_i^\beta[k+1] = \left(\lambda_i^\beta[k] + \theta_k \underbrace{\delta_i^\beta(\vec{x}^*[k], \vec{y}^*[k], \vec{t}^*[k], \vec{\beta}^*[k])}_{\delta_i^\beta[k]} \right)_+, \quad (18a)$$

$$\lambda_i^\tau[k+1] = \left(\lambda_i^\tau[k] + \theta_k \underbrace{\delta_i^\tau(\vec{x}^*[k], \vec{y}^*[k], \vec{t}^*[k], \vec{\tau}^*[k])}_{\delta_i^\tau[k]} \right)_+. \quad (18b)$$

Here, $\vec{x}^*[k], \vec{y}^*[k], \vec{t}^*[k], \vec{\beta}^*[k], \vec{\tau}^*[k]$ are the solutions of the computed from the subproblems (16), (15a), and (15b) with $\vec{\lambda}[k]$. The values $\delta_i^\beta[k]$ and $\delta_i^\tau[k]$ are thus the corresponding subgradients of $D(\vec{\lambda})$ for each component. The notation $(a)_+$ denotes $\max\{0, a\}$. The step size at k -th iteration is denoted as θ_k .

The overall algorithm is summarized in Algorithm 1. From a high-level perspective, the dual variables $\vec{\lambda}$ can be interpreted as the price for the scheduled deadline and SoC. For example, a higher λ_i^β gives more weight on the constraint δ_i^β and has multiple effects. First, it gives more weight for the energy cost in (13), thus resulting in a larger traveling time in the edge subproblem (15a). Meanwhile, a higher λ_i^β results in a lower scheduled SoC β_o^i at i -th stop but a higher β_o^{i-1} and more charging time $t_c^{i,v}$ at $(i-1)$ -th stop. It means that a higher λ_i^β results in a larger difference of scheduled SoC between charging stops $(i-1)$ and i . A similar interpretation applies to the dual variable λ_i^τ . Overall, Alg. 1 seeks to find a solution that balances the objective and the constraint cost and adjusts the dual variable via the subgradient direction.

4.3 Performance Analysis

In this subsection, as one of the key contributions, we show that (i) our algorithm always converges with a rate of $O(1/\sqrt{K})$ where K is the number of iteration, (ii) each iteration only incurs polynomial-time complexity in graph size, and (iii) it generates optimal results if a condition is met and solutions with bounded loss otherwise.

Convergence Rate. Similar to standard subgradient methods [14], algorithm 1 also converges to dual optimal value at a rate of $O(1/\sqrt{K})$.

THEOREM 4.2. *Let D^* be the optimal dual objective and let \bar{D}_K be the maximum dual value over K iterations in algorithm 1. With constant step size $\theta_k = \frac{1}{\sqrt{K}}$, we have, for some constant C ,*

$$D^* - \bar{D}_K \leq \frac{C}{\sqrt{K}}. \quad (19)$$

It shows that a constant step size $\theta_k = 1/\sqrt{K}$ is sufficient to achieve a convergence rate of $O(1/\sqrt{K})$. However, one may achieve better empirical convergence by adaptively updating the step sizes [9]. Besides, another improvement can be achieved by modifying the subgradient directions [15].

Time Complexity. We summarize the time complexity analysis of Alg. 1 in the following Proposition.

PROPOSITION 4.3. *The time complexity per iteration of Alg. 1 is*

$$O\left((N+1)|\mathcal{V}_c||\mathcal{V}||\mathcal{E}| + N|\mathcal{V}_c| \frac{M^4}{\epsilon_1^4}\right) \quad (20)$$

, where $M = \{t_c^{ub}, t_w^{ub}, B, T\}$ and ϵ_1 is the required accuracy for solving the subproblems (15b)

Proposition 4.3 states that at each iteration, Alg. 1 incurs only polynomial time complexity in graph size, albeit it requires solving the ILP subproblem in (15b) optimally. Meanwhile, Theorem 4.2 guarantees that Alg. 1 converges to a solution with accuracy ϵ_0 in $O(1/\epsilon_0^2)$ iterations. We can derive the total time complexity of Alg. 1 by combining Proposition 4.3 and Theorem 4.2.

Optimality Gap. Note that in the dual subgradient method, a convergence to dual optimal does not imply a convergence to the primal optimal as there might be a duality gap. To this end, we provide the following bound on the optimality gap.

THEOREM 4.4. *Let OPT be the optimal objective to the problem in (10). If Alg. 1 produces a feasible solution updated at iteration k with objective ALG , then the optimality gap is bounded by*

$$ALG - OPT \leq - \sum_{i=1}^{N+1} \left(\lambda_i^\beta[k] \delta_i^\beta[k] + \lambda_i^\tau[k] \delta_i^\tau[k] \right). \quad (21)$$

The posterior bound (21) simply comes from the weak duality. Meanwhile, we can compute it at each iteration in Alg. 1 and use it for early termination upon certain accuracy. Moreover, Theorem 4.4 also provides an optimality condition of the produced solution by the following corollary.

COROLLARY 4.5. *If Alg. 1 returns a feasible solution in line 5, then the solution is optimal.*

Note that Theorem 4.4 requires Alg.1 to produce a feasible solution, which is not guaranteed in dual-based methods. In the case where Alg.1 does not find a feasible solution, we re-optimize the speed planning and charging planning with the given path in the last iteration of Alg. 1 and try to recover a feasible primal solution. As seen in Sec. 5, this recovery scheme always finds a feasible solution.

5 NUMERICAL EXPERIMENTS

In this section, we evaluate the performance of our algorithm by simulations using real-world traces over the US highway network.

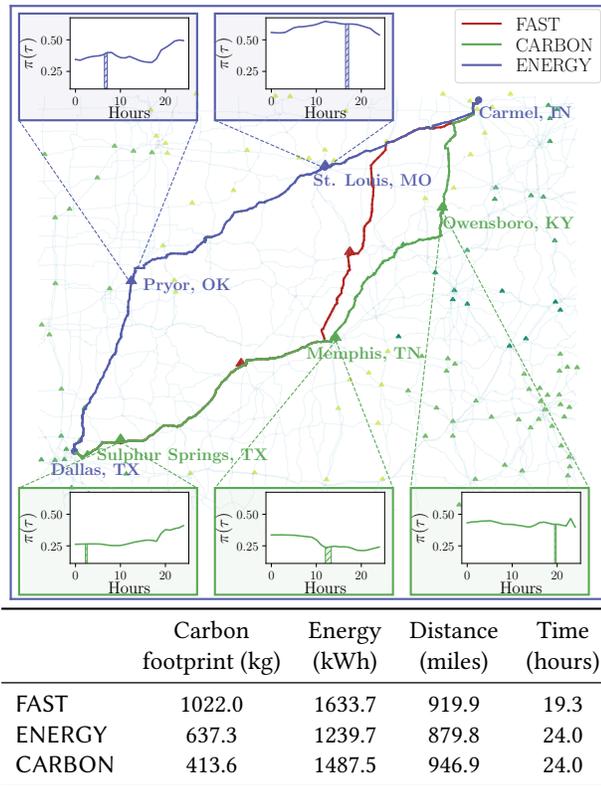


Figure 5: The illustration of carbon-optimized and energy-optimized solutions from Dallas, TX to Carmel, IN. In the figure, the shaded area represents the period of charging process.

Our objectives are (i) to study the behavior of the carbon-optimized solutions. (ii) to study the performance of the proposed approach as compare to baselines and the impact of path planning, speed planning, charging planning, respectively; (iii) to study the impact of conservative ratio α ; (iv) to compare the carbon footprint between electric trucks and ICE trucks, and study the environmental benefit of electric trucks.

5.1 Experiment Setup

Transportation network. We collect the highway network data from the Map-based Educational Tools for Algorithm Learning (METAL) project [49]. The constructed network consists of 84,504 nodes and 178,238 directed edges. We collect the real-time road speed data from HERE map [40]. The grade of each road segment is derived from the elevations of its end nodes provided by the Shuttle Radar Topography Mission (SRTM) [22] project. We also pre-process the road network and merge the adjacent road segments with similar grades with tolerance 0.5% to reduce the computational complexity.

Energy consumption model. We use the simulator *FASTSim* [27] to collect the energy consumption data with driving speed (from 10 mph to 70 mph with a step of 0.2 mph) at different grades (from -6% to 6% with a step of 0.25%)³. Then we fit the energy consumption

³We note that the maximum grade allowed for the inter-state highway is a 6-meter difference in elevation every 100 meters road length in the United States [28].

Origin	Destination	Distance (miles)	Value (billion USD)
Los Angeles CA	Columbus OH	1977	17.725
Los Angeles CA	Dallas-Fort Worth TX	1240	12.247
Los Angeles CA	Chicago IL	1745	11.293
Los Angeles CA	Nashville TN	1780	10.718
Los Angeles CA	Houston TX	1373	7.837

Table 4: Five popular origin-destination pairs from Los Angeles.

data with cubic polynomial functions. We use the parameters of Tesla Semi [50] for the electric truck model with the battery capacity $B = 1,000$ kWh and the total weight of 36 tons. We assume the e-truck is fully charged at the origin, i.e., $\beta_0 = B$.

Origin-destination pair. We collect origin-destination pairs from the Freight Analysis Framework (FAF) [33]. We select 500 origin-destination pairs with distances longer than 800 miles. Those pairs represent 950 billion dollars of freight by trucks in 2017. Tab. 4 illustrates a subset of the selected origin-destination pairs in the US starting from Los Angeles.

Charging station data. We collect the location data of charging stations from the OpenStreetMap (OSM) [42] and add each location to the nearest road segment in the constructed graph. The collected data yields 2,555 charging stations. We approximate the charging functions with a piecewise linear function using six break points at 0%, 80%, 85%, 90%, 95%, 100% SoC [6]. The resulting charging function can charge the studied electric truck from 0% to 80% in 48 minutes. See Fig.2 for an illustration. We collect the electricity generation data from Energy Information Administration (EIA) [20] and obtain a piecewise linear carbon intensity function $\pi(\cdot)$ for each charging station (See Fig. 1).

In the simulation, we implement and compare the following conceivable alternatives.

- ▷ CARBON: our carbon footprint minimizing approach.
- ▷ ENERGY: our approach with the objective of minimizing energy consumption by setting the carbon intensity function $\pi(\cdot) \equiv 1$.
- ▷ FAST: our approach with the objective of minimizing total travel and charging time by changing the objective and following the similar dualization procedure in Sec. 4.
- ▷ FAST-S: the same path of FAST with the speed planning.
- ▷ FAST-SC: the same path of FAST with the speed planning and charge planning.

5.2 Behavior of Carbon-Optimized Solution

We first study a transportation task from Dallas, TX to Carmel, IN. We compare the solution of FAST, CARBON and ENERGY and present them in Fig. 5. We observe that CARBON tends to "follow the sun and go with the wind" to charge the electricity with the low carbon intensity and achieves a 59.6% carbon reduction as compared to FAST and 35.2% as compared to ENERGY. To achieve such a large carbon reduction, CARBON charge a small amount of energy at the first and the third charging station to ensure the sufficient SoC on road while charge more at the second charging station for lower carbon footprint. Meanwhile, the detour to the greener charging station leads to a slightly longer total distance and slightly more energy consumption as compared to the energy-optimized

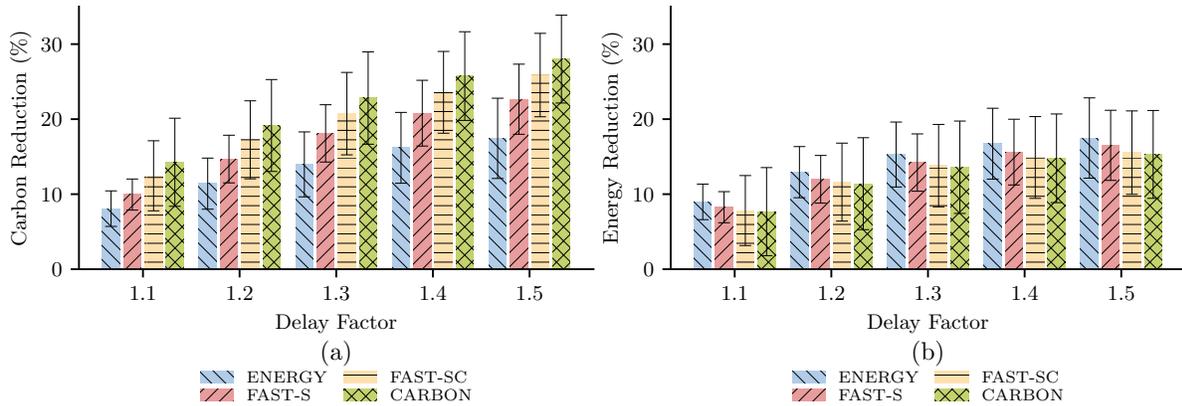


Figure 6: Simulation results for 500 instances. The carbon (energy) reduction is also computed with respect to FAST.

solution. We find similar observations in the next subsection where we conduct the simulation over all 500 origin-destinations.

5.3 Comparison with Baselines

We then conduct simulations on 500 origin destination pairs. For each pair, we denote by T_f the total travel time of FAST and set deadlines from $1.1T_f$ to $1.5T_f$. We call the ratio between the deadline and T_f the *delay factor*. The start time is set to 4 PM, Jan 1st, 2022. We set the number of charging stops N of CARBON and ENERGY the same as FAST. In these typical settings, the number of charging stops is no more than eight. We set the ratio of conservative lower bound $\alpha = 0.05$. CARBON produces feasible solutions for 96% of all instances. For infeasible solutions, we increase α until it produces a feasible solution. A maximum value of $\alpha = 0.12$ guarantees CARBON to produce feasible solutions for all instances.

We show the simulation results in Fig. 6. All the results are mean values over 500 origin-destination pairs and the error bars represent the standard deviations. Fig. 6(a) and Fig. 6(b) give the the carbon (resp. energy) reduction of different baselines as compared to FAST. We observe that as the deadline gets relaxed, the carbon (and energy) reduction of all the baselines increases. Moreover, different components of the design space contribute differently into such reduction as we shall discuss in the following.

Benefit of Carbon-Optimized Solution. We first compare CARBON and ENERGY. As shown in Fig. 6(a), while the carbon footprint of both approaches decrease as the deadline increases, CARBON benefits more from the relaxed deadline and achieves higher carbon reduction. In particular, CARBON achieves 19% carbon reduction as compared to FAST baseline under the typical setting when the delay factor is 1.2 and up to 28% when the delay factor is 1.5. Meanwhile, as compared to its energy-efficient counterpart ENERGY, CARBON achieves 9% carbon reduction when the delay factor is 1.2 and 13% when the delay factor is 1.5. This difference mainly comes from the fact that minimizing energy simply ignores the temporal diversity of the renewable and loses part of the optimization space. Therefore, minimizing energy consumption does not necessarily lead to a minimum carbon footprint. It is essential to consider the carbon footprint objective when studying the environmental impact of e-trucks. Meanwhile, we also observe from Fig. 6(b)

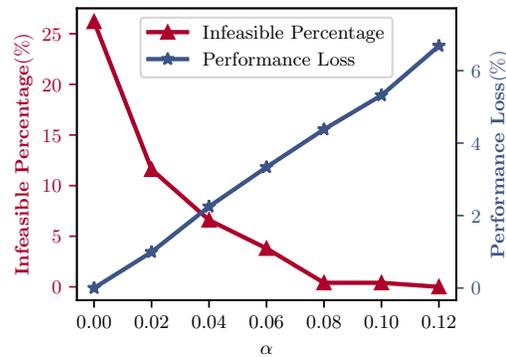


Figure 7: Impact of conservative ratio α .

that the difference of energy reduction between CARBON and ENERGY is less than 3%. This means that a carbon-efficient route is also energy-efficient.

Impact of Speed Planning. We then investigate FAST-S to study the impact of speed planning. When the delay factor is 1.2, FAST-S saves 15% carbon footprint and 12% energy as compared to FAST. As compared to ENERGY, FAST-S saves 3% additional carbon footprint. This additional saving comes from the fact that the optimized speed plan re-schedules the travel time of each stage such that the e-truck charges greener electricity at each stage.

Impact of Charging Planning. We then compare FAST-S and FAST-SC to study the impact of charging planning. We observe that when the delay factor is 1.2, FAST-SC saves 2.5% additional carbon footprint as compared to FAST-S because FAST-SC takes the advantage of charging planning such that the e-truck can wait for the lower carbon intensity.

Impact of Path Planning. We then compare FAST-SC and CARBON to study the impact of path planning. We observe that when the delay factor is 1.2, CARBON saves 2% additional carbon footprint as compared to FAST-SC because e-truck can select greener charging stations with path planning.

5.4 Impact of Conservative Ratio α

In this subsection, we study the impact of the conservative ratio α . We run CARBON on 500 origin-destination pairs for α ranging

Delay Factor	1.1	1.2	1.3	1.4	1.5
ENERGY	50.8%	51.4%	52.4%	53.6%	54.1%
CARBON	54.7%	55.9%	57.1%	58.3%	59.2%

Table 5: Average carbon reduction with respect to ICE truck over 500 origin-destination pairs.

from 0.0 to 0.12. For each α , we check the SoC at each road segment of the solutions and report the percentage of solutions violating positive SoC among all 500 origin-destination pairs. In addition, we notice that CFO with $\alpha = 0$ (named CFO₀) provides a lower bound to the CFO with positive SoC constraints at all road segments but no reservation requirement. We thus define performance loss of CARBON with CFO as its relative error with respect to the CARBON with CFO₀, i.e.,

$$\text{Performance Loss} = \frac{ALG_{\alpha} - ALG_0}{ALG_0},$$

where ALG_{α} is the objective value of solutions by CARBON for CFO. The results are presented in Fig. 7. We observe that when $\alpha = 0$, there are 26% of infeasible solutions while a small increment of α leads to a large feasibility improvement, e.g., $\alpha = 0.02$ with 12% of infeasible solutions. We observe that $\alpha = 0.12$ is sufficient to guarantee feasibility for all 500 origin-destination pairs. Meanwhile, we observe the performance loss introduced by α grows almost linearly with respect to α . In a typical selection when $\alpha = 0.06$, 96% of solutions are feasible while the performance loss is only 3.3%. In the most conservative case when $\alpha = 0.12$ that guarantees the feasibility of all the solutions, the performance loss is 6.7%. Thus, by introducing the conservative ratio α , we significantly simplify the coupling SoC constraint while ensuring feasibility with minor performance loss.

5.5 Comparison with ICE Trucks

In this subsection, we study the environmental benefits of electric trucks as compared to ICE trucks. We use the parameters of Kenworth T800 trailer [35] for the ICE truck model with the same total weight of 36 tons. For the ICE truck, we compute the energy-efficient path plan and speed plan by the dual-based method in [18]. We use the CO₂ factor value of diesel from EIA [1] to transform the fuel consumption of the ICE truck to its direct carbon emission. The data suggest that if an ICE truck is powered by diesel, it will produce 9.88 kg CO₂ per gallon, or equivalently 0.25 kg CO₂ emission per kWh. The simulation results are presented in Tab. 5. We observe that the e-truck saves 55.9% carbon as compared to the ICE truck under a delay factor 1.2.

There are several factors that contribute to such carbon reduction. First, e-trucks consume less energy due to the high efficiency of electric motors and the regenerative braking system. Second, with the increasing integration of renewable generations for e-truck charging, the carbon footprint of an electric truck reduces. Third, our joint optimization of path planning, speed planning and charging planning leads an e-truck to charge clean electricity with low carbon intensity. Overall, these factors together lead to a significant reduction of the carbon footprint of the electric truck as compared to the ICE truck.

6 DISCUSSION

Battery Degradation. The modeling and prediction of battery degradation is in general difficult and still an active research area [32]. Among many factors that affects the battery degradation, the most relevant ones for the transportation tasks are charge or discharge rate and the depth of discharge (DoD) [43]. A high charge rate or a high DoD may accelerate the battery degradation. To prolong the battery lifetime, we can add a battery degradation cost in the objective. We can model different charging mode by adding multiple charging stations at the same location, where a charging mode with the higher rate incur higher degradation cost. To prevent large DoD, we can also add a degradation cost if the arrival SoC is lower than certain value.

Dynamic Traffic Condition. In the real world, the traffic conditions can be time-varying. To adapt variable traffic conditions in our formulation, we can incorporate the phase-based traffic model [52] into our stage-expanded graph, where the traffic condition is approximately static at each phase. Then we can treat the combination of the stage and the traffic phase as the new stage and apply our approach.

Applications Beyond CFO. We remark that our approach has applications beyond this paper. For example, it is also applicable to general routing problem for electric/ICE vehicles with energy consumption and monetary objective. Our approach is also applicable to the subproblem for electric vehicle routing problem (EVRP) in a branch-price-and-cut framework [19].

7 CONCLUSION

In this paper, we present the first study in the literature on the *Carbon Footprint Optimization* (CFO) problem of a heavy-duty e-truck traveling from an origin to a destination across a national highway network subject to a hard deadline, by optimizing path planning, speed planning, and intermediary charging planning. We show that the problem is NP-hard and under practical settings it is equivalent to finding a generalized RSP on a novel stage-expanded graph, which extends the original transportation graph to model charging options. Our problem formulation incurs low model complexity and reveals a problem structure that leads us to an efficient dual-subgradient algorithm with a strong performance guarantee. Extensive simulation results over the US national highway network show that our solutions reduce up to 28% carbon footprint compared to the baseline alternatives. The results also demonstrate the carbon efficiency of e-trucks over ICE trucks.

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